Chlorine Nuclear Spin-Spin Relaxation Mechanism in Mg(H₂O)₆SnCl₆ as Studied by NQR and NMR Techniques*

Keizo Horiuchi

Department of Chemistry, Division of General Education, University of the Ryukyus, Nishihara, Okinawa 903-01, Japan

Daiyu Nakamura^a

Department of Chemistry, Faculty of Science, Nagoya University, Chikusa, Nagoya 464-01, Japan

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The 35 Cl NQR spin-lattice relaxation time T_{1Q} , spin-spin-relaxation time T_{2Q} , and 1 H NMR spin-lattice relaxation time in the rotating frame T_{1q} in Mg(H₂O)₆SnCl₆ were measured as functions of temperature. Above room temperature T_{2Q} increased rapidly with increasing temperature, which can be explained by fluctuations of the local magnetic field at the chlorine nuclei due to cationic motions. From the T_{1q} experiments, these motions are found to be attributable to uniaxial and overall reorientations of [Mg(H₂O)₆]²⁺ ions with activation energies of 95 and 116 kJ mol⁻¹, respectively. Above ca. 350 K, T_{1Q} decreased rapidly with increasing temperature, which indicates a reorientational motion of [SnCl₆]²⁻ ions with an activation energy of 115 kJ mol⁻¹.

Key words: Complex compounds, Molecular dynamics, Nuclear relaxation, Nuclear quadrupole resonance, Nuclear magnetic resonance.

Introduction

Previously, we studied the temperature variation of the ³⁵Cl NQR frequencies in M(II)(H₂O)₆SnCl₆ (M(II) = Ca, Mg, Mn, Co, Ni) and $M(II)(D_2O)_6SnCl_6(M(II)$ = Ca, Co, Ni) crystals [1]. The crystal structure of the Ni and the Ca salts at room temperature were determined by X-ray diffraction measurements [2, 3]. The crystals were found to be trigonal with a space group $R\overline{3}$ and the slightly distorted CsCl type structure consisting of an [M(II)(H₂O)₆]²⁺ octahedron and an [SnCl₆]²⁻ octahedron. The other compounds are isomorphous with the two salts [1]. All these complexes yielded a single ³⁵Cl NOR signal and showed unusual temperature dependences with a positive temperature coefficient [1], which were assigned to weak Cl ⋅ ⋅ · H−O type hydrogen bonds [1]. In these compounds three hydrogen atoms are close to a chlorine atom. These Cl · · · O bond distances are 3.344, 3.352, and 3.550 Å in $Ca(H_2O)_6SnCl_6$ [3].

Recently, we have studied the dynamics of molecular ions in pyridinium tetrachloroaurate (III) and pyridinium hexachlorometallates (IV) by chlorine NQR and proton NMR experiments [4–7]. In these complexes, an unusual relaxation mechanism was found on measuring the 35 Cl NQR spin-lattice relaxation time T_{1Q} and the 1 H NMR spin-lattice relaxation time T_{1} . That is, it was shown that the relaxation mechanisms of the chlorine and hydrogen nuclei are fluctuations of the electric field gradient (EFG) due to cationic motions and fluctuations of the local magnetic field due to anionic motions, respectively.

In the present work, the 35 Cl NQR T_{1Q} and spinspin relaxation time T_{2Q} , and the 1 H NMR spin-lattice relaxation time in the rotating frame T_{1Q} were measured as functions of temperature. By these measurements, we can investigate whether the fluctuation (modulation) of inter-nuclear interactions due to cationic motions affects the chlorine nuclear relaxation mechanism in $Mg(H_2O)_6SnCl_6$.

a Deceased.

Reprint requests to Dr. Keizo Horiuchi, Department of Chemistry, Division of General Education, University of the Ryukyus, Nishihara, Okinawa, 903-01, Japan.

Experimental

The sample was synthesized in the same way as described in [1]. For the NQR measurements, the polycrystalline sample was sealed in a glass tube and

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annealed at ca. 410 K for 24 hours to strengthen the intensity of the NQR signal. For the NMR measurements the sample was powdered and dried in a desiccator with silica gel for one day before being sealed in a sample tube.

 $T_{1\rm Q}$ and $T_{2\rm Q}$ were measured by means of a pulsed NQR spectrometer [8]. The temperature of the specimen was controlled within ± 0.5 K, and determined with an accuracy of ± 1 K. $T_{1\rm Q}$ was determined by a $180^\circ - \tau - 90^\circ - \tau_{\rm e} - 180^\circ$ pulse sequence, in which $\tau_{\rm e}$ was fixed throughout a measurement at $200 - 400~\mu \rm s$ and $T_{2\rm Q}$ by a $90^\circ - \tau - 180^\circ$ pulse sequence.

The measurements of $T_{1\varrho}$ were made by employing a standard spin-locking technique [9]. The Larmor frequency was 32 MHz and the spin-locking field 6.8 G. The sample temperature was estimated to be accurate within ± 1 K.

Results

The obtained 35 Cl NQR T_{1Q} and T_{2Q} in Mg(H₂O)₆SnCl₆ are shown in Figure 1. The most interesting feature is the temperature variation of T_{2Q} above room temperature. T_{2Q} below 167 K was almost constant (ca. 450 µs). Above 167 K, T_{2Q} increased very slowly on heating. However, between 250 and 345 K T_{2Q} showed a nearly constant value of ca. 580 µs. When the temperature increased further, T_{2Q} increased rapidly and then exhibited a sharp maximum (1.29 ms) around 390 K. Between 352 and 366 K, log T_{2Q} depended linearly on T^{-1} . With further increasing temperature T_{2Q} decreased steeply. The temperature dependence of T_{2Q} above ca. 330 K is shown in detail in an insert of Figure 1.

The temperature variation of T_{1Q} is divided roughly into two regions. Above ca. 350 K T_{1Q} decreases very rapidly with increasing temperature and $\log T_{1Q}$ vs. T^{-1} plots are almost linear between ca. 370 and 420 K. Below ca. 350 K T_{1Q} increases gradually with decreasing temperature.

The 1 H NMR free induction decay (FID) signal in Mg(H₂O)₆SnCl₆ at room temperature can be interpreted in terms of a typical dipolar interacting two-proton system. With increasing temperature the FID shape changed gradually, and above ca. 360 K the FID signal decayed monotonously. Figure 2 shows the temperature dependence of the 1 H NMR $T_{1\varrho}$ between 295 and 495 K. The log $T_{1\varrho}$ vs. T^{-1} curve yields a broad and unsymmetrical minimum around 380 K.

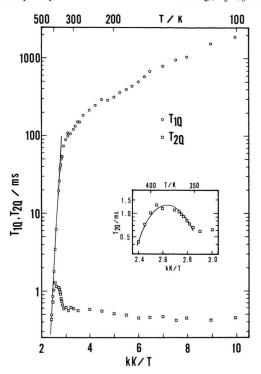


Fig. 1. Temperature dependence of the 35 Cl NQR spin-lattice relaxation time T_{1Q} , and spin-spin relaxation time T_{2Q} in Mg(H₂O)₆SnCl₆. In the inset, the T_{2Q} values above ca. 330 K are plotted in detail against the inverse temperature drawn to large scale. The solid line indicates the best fitted curve.

 $T_{1\varrho} \approx 120~\mu s$ between 370 and 420 K. The temperature dependence of $T_{1\varrho}$ at the high temperature side of the minimum is slightly steeper than that at the low temperature side.

Discussion

 ^{1}H NMR Spin-Lattice Relaxation Time in the Rotating Frame $T_{1\varrho}$

In general, $T_{1\rho}$ is expressed as

$$T_{1\varrho^{-1}}^{-1} = \sum_{i} C_{i} \left(\frac{3}{2} \frac{\tau_{ci}}{1 + 4\omega_{1}^{2} \tau_{ci}^{2}} + \frac{5}{2} \frac{\tau_{ci}}{1 + \omega_{0}^{2} \tau_{ci}^{2}} + \frac{\tau_{ci}}{1 + 4\omega_{0}^{2} \tau_{ci}^{2}} \right), \tag{1}$$

where ω_0 is the angular resonance frequency of the nucleus and $\omega_1 = \gamma H_1$, γ is the nuclear gyromagnetic ratio and H_1 is a spin locking field [10]. C_i is the *i*-th motional constant, which is related to the second mo-

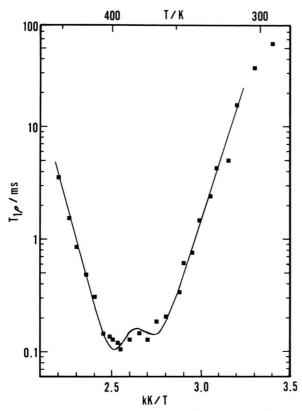


Fig. 2. Temperature dependence of the $^1\mathrm{H}$ NMR spin-lattice relaxation time in the rotating frame $T_{1\varrho}$ in Mg(H₂O)₆SnCl₆. The resonance frequency v_0 is 32 MHz and the spin-locking field H₁ is 6.8 G. The solid line represents the best fitted curve

ments reduction ΔM_{2i} caused by the *i*-th motional mode [11]:

$$C_i = (2/3)\gamma^2 \Delta M_{2i}. \tag{2}$$

According to the measurements of the ^{1}H NMR second moments M_{2} [12], it decreases from 23.6 G^{2} at ca. 330 K to 1.8 G^{2} at 412 K. This second moments reduction can be related to the observed $T_{1\varrho}$ minimum. The temperature variation of the shape of the FID signal is considered to result from an averaging of the dipolar interaction between a pair of protons in a water molecule. Moreover, from the fact that M_{2} decreases to a very small value we can assume that a Brownian motion of the proton pair is activated. The motional constant for this mode is given by

$$C = \frac{2}{5} \frac{\gamma^4 \, \hbar^2}{r^6} I(I+1),\tag{3}$$

where r is the inter-nuclear distance and I the nuclear spin quantum number [13]. We assume that the distance of two protons is 1.6 Å, which is the normal value in a water molecular and also the value reported for $Ca(H_2O)_6SnCl_6$ [3]. With this value, ΔM_2 is calculated to be 21.3 G^2 from (2) and (3). This value agrees quite well with the observed value of 22 ± 3 G^2 .

By use of the observed ΔM_2 value, we can calculate the minimum value of $T_{1\varrho}$ from (1). The value of $22~G^2$ leads to $T_{1\varrho, \min} = 47~\mu s$, which does not agree with the measured value of ca. 100 μs . Moreover, judging from the unsymmetrical minimum of the $T_{1\varrho}$ curve it is very hard to interpret this result by a single motional mode. Hence we tentatively assume that two motional modes are activated above room temperature. Since the term containing ω_1 is dominant in (1) around the temperature at which the $T_{1\varrho}$ minimum is observed, we have calculated the least squares fit of the equation

$$T_{1\varrho}^{-1} = a_1 \frac{\tau_{01} \exp(E_{a1}/RT)}{1 + 4\omega_1^2 \left[\tau_{01} \exp(E_{a1}/RT)\right]^2} + a_2 \frac{\tau_{02} \exp(E_{a2}/RT)}{1 + 4\omega_1^2 \left[\tau_{02} \exp(E_{a2}/RT)\right]^2}, \quad (4)$$

where $a_i(=\gamma^2\Delta M_{2i})$, τ_{0i} , and E_{ai} (i=1,2) are fitting parameters and $\omega_1=2\,\pi\times29$ kHz. The resulting best fitted curve is depicted in Fig. 2, and the obtained numerical values are listed in Table 1. The sum of $(\Delta M_2)_{\rm fit}$ obtained from this fitting calculation was $15.1\pm4\,{\rm G}^2$, which agrees with the observed ΔM_2 value of $22\pm3\,{\rm G}^2$ within the experimental errors. From this result we conclude that two motional modes of cations are activated above room temperature.

The same features were also reported for $Ca(H_2O)_6SnCl_6$ [14], in which the motions with a low and a high activation energy were identified as a reorientation about the C_3 or C_4 axes and an isotropic tumbling motion of the entire cation, respectively. We also adopt this identification for the present compound. The activation energy of the uniaxial motion derived from T_1 measurements was 83 ± 5 kJ mol [12], which agrees well with our result of 95 ± 10 kJ mol⁻¹.

The activation energies observed for the Ca complex were 38 and 48 kJ mol⁻¹ for the uniaxial and the overall reorientation, respectively [14]. These values are only 40% of those of the present complex. Since these two compounds are isomorphous, such energy differences seem to be too large. However these energy

Table 1. Motional parameters of $[Mg(H_2O)_6]^{2+}$ ions and $[SnCl_6]^{2-}$ ions in $Mg(H_2O)_6SnCl_6$. These values were determined by the fitting calculation of 1H NMR $T_{1\varrho}$ and ^{35}Cl NQR T_{1O} data.

Motional mode	$a \times 10^{9}/s^{-2}$	$E_{\rm a}/{\rm kJ~mol^{-1}}$	τ_0/s
H ₂ O 180° flips Cation C ₃ or C ₄ Cation overall Anion reorient.	4.6 6.2	$22\pm2*$ 95 ± 10 116 ± 6 115 ± 4	$7.0 \times 10^{-15} *$ 6.4×10^{-20} 1.6×10^{-21} 3.5×10^{-18}

^{*} Ref. [12].

differences agree with the fact that the Ca complex is much more hygroscopic than the Mg one.

Furthermore we find that the τ_0 values obtained for the cationic motions are very small. Analyzing the $T_{1\varrho}$ data, the correlation time of the motion τ_c could be expressed as

$$\tau_{\rm c} = \tau_0 \exp(E_{\rm a}/RT). \tag{5a}$$

To be more exact, however, $\tau_{\rm c}$ should be expressed as

$$\tau_{\rm c} = \tau_0' \exp(\Delta G_{\rm a}/RT), \tag{5b}$$

where $\Delta G_a = \Delta H_a - T\Delta S_a$ is the free energy of activation. In $\Delta H_a = E_a - RT$, RT is negligible compared with ΔH_a and E_a . Hence from (5a) and (5b) we get

$$\tau_0 = \tau_0' \exp\left(-\Delta S_a/R\right). \tag{5c}$$

This relation shows that the small value of τ_0 results from an entropy effect. In the present compound, site disorders of hydrogens and/or oxygens of cations are considered to bring about this effect.

³⁵Cl NQR Spin-Spin Relaxation Time T₂₀

Above room temperature, $T_{\rm 2Q}$ showed a drastic temperature variation. In general, if the fluctuation of interactions caused by lattice vibrations is responsible for the nuclear relaxation mechanism, $T_{\rm 2Q}$ scarcely varies with temperature [8, 15]. Therefore another relaxation mechanism is thought to exist in $Mg(H_2O)_6SnCl_6$.

Generally speaking, T_{2Q} consists of an adiabatic (secular) part $T_{2Q, \text{ adiab}}$ and a non-adiabatic (non-secular) part $T_{2Q, \text{ non-adiab}}$ [16]:

$$T_{20}^{-1} = T_{20, \text{adiab}}^{-1} + T_{20, \text{non-adiab}}^{-1}$$
 (6)

The observed steep decrease of $T_{\rm 2Q}$ with increasing temperature above 400 K can be explained in terms of the non-adiabatic part because in this temperature

region T_{1Q} is nearly equal to T_{2Q} . These temperature variations of T_{1Q} and T_{2Q} above 400 K result from a reorientational motion of the anions [17].

Below 370 K, however, T_{1Q} is longer than T_{2Q} , and so the adiabatic part must be dominant in T_{2Q} . Moreover, we find that the observed temperature dependence of T_{20} below 370 K is very similar to the one observed in NMR experiments [18]. According to the BPP theory, this temperature dependence of T_2 arises from the secular part and is explained as follows. We assume that the fluctuation of the inter-nuclear interactions due to a molecular motion is the dominant relaxation mechanism. When the correlation time of the motion τ_c is longer than T_2'' (T_2'' being the time characterizing the spin-spin coupling in the rigid lattice and being nearly equal to the inverse of the linewidth) then $T_2 = T_2'' = \text{const.}$ Since τ_c decreases with increasing temperature, it becomes shorter than T_2'' at some temperature. Above this temperature, the inter-nuclear interactions are averaged by this motion, and T_2 increases linearly with τ_c^{-1} with increasing temperature (motional narrowing). Hence, we find that $\log T_2$ depends linearly on T^{-1} as long as the motional correlation time can be expressed by (5a). Judging from the similarity between the temperature dependence of T_2 and the observed one of T_{20} below 370 K, we can infer that in Mg(H₂O)₆SnCl₆ there exists the same relaxation mechanism as mentioned above.

Among the motional modes thought to exist in this complex, anionic motions cannot be responsible for this relaxation mechanism. The reason is as follows. If the reorientational motion of the ions containing the resonant nuclei is effective on the spin-lattice relaxation, T_{10} becomes nearly equal to τ_c [17]. Hence around the temperature at which τ_c becomes shorter than T_{20}'' , T_{10} already decreases to the value nearly equal to T_{2Q} and the non-adiabatic part dominates in T_{20} . In this case T_{20} decreases with increasing temperature as observed in general [8]. On the other hand, cationic motions can be responsible for the temperature dependence of T_{20} . Furthermore, from the measurements of $T_{1\rho}$ we have found that two motions of cations are activated above room temperature in this compound. These motions could be responsible for the chlorine nuclear relaxation.

The rapid increase of T_{2Q} and the decrease of the ¹H NMR M_2 with increasing temperature occurred at nearly the same temperature of ca. 340 K. The correlation time of the uniaxial motions around this temper-

ature is ca. 10^{-4} s, which satisfies the motional narrowing condition. These results suggest that the same cationic motions are responsible for the temperature variation of T_{2Q} and M_2 above room temperature. Therefore we can conclude that the temperature dependence of T_{2Q} below 370 K is caused by the modulation effect due to the cationic motions.

Next, let us examine whether magnetic interactions can be responsible for $T_{\rm 2Q}$ observed below 370 K. It is difficult to calculate exactly the local magnetic field $H_{\rm loc}$ at a chlorine nucleus, so we are satisfied with estimating an order of $T_{\rm 2Q}^{\prime\prime}$. In this case, it is enough to take into account only $H_{\rm loc}$ produced by three protons close to the chlorine nuclei. A rough estimate for $T_{\rm 2Q}^{\prime\prime}$ due to the magnetic interactions is given by

$$(T_{2O}'')^{-1} = \gamma_{Cl} H_{loc} = \gamma_{Cl} \gamma_{H} \hbar / r^{3},$$
 (7)

where γ_{Cl} and γ_{H} are the gyromagnetic ratio of the chlorine nucleus and the proton, respectively, and r is the inter-nuclear distance [19]. On the basis of the reported value of the O...Cl bond distance in $Ca(H_2O)_6SnCl_6$ [3], we can assume r = 2.6 Å. This value gives $T_{20}'' = 0.08$ ms, which is somewhat shorter than the measured value of 0.45 ms below ca. 170 K. This difference is considered to be partly caused by the averaging due to the motion of water molecules and partly to lattice vibrations of anions. Accordingly, it can be concluded that the T_{20} values below 370 K are attributed to the magnetic interactions between chlorine nuclei and protons of the cations. In some T_{10} measurements of the 14N NQR, a distinct minimum such as observed in NMR [18] was observed [20]. Such a minimum has been interpreted, in the same way as discussed above, in terms of the fluctuation of the dipolar field caused by the reorientation of nearby groups containing nuclei which produce the dipolar field at the resonant nuclei.

On carefully looking at the $T_{\rm 2Q}$ results shown in the insert of Fig. 1, we find that in the temperature region between 370 and 400 K, $T_{\rm 2Q}$ is nearly constant. This seems to result from the fluctuation due to lattice vibrations being effective over other relaxation mechanism in this temperature region. Hence in all three relaxation mechanisms probably contribute to $T_{\rm 2Q}$ in $Mg(H_2O)_6SnCl_6$:

$$T_{2O}^{-1} = T_{2O, latt}^{-1} + T_{2O, mod}^{-1} + T_{2O, recrient}^{-1}$$
 (8)

Here, $T_{\rm 2Q, \, latt}$, $T_{\rm 2Q, \, mod}$, and $T_{\rm 2Q, \, reorient}$ are the spin-spin relaxation times due to lattice vibrations, the cationic motions, and the anionic motions, respectively. In or-

der to estimate $T_{2Q, latt}$, we will fit the above equation to the T_{2Q} data.

 $T_{20, latt}$ is assumed to take a constant value,

$$T_{20, \text{ latt}}^{-1} = b.$$
 (9 a)

In the temperature region where $T_{2Q, \, \text{mod}}$ is dominant, the correlation time of the uniaxial motion is faster than that of the overall reorientation, so it is adequate to consider only the contribution from the C_3 or C_4 reorientations,

$$T_{20, \text{mod}}^{-1} = d\tau_{c2},$$
 (9b)

where τ_{c2} is the correlation time of the uniaxial motion of cations.

Above 400 K, T_{2Q} is nearly equal to T_{1Q} , so we can assume

$$T_{2O, \text{ regrient}} = P \tau_{ca},$$
 (9 c)

where τ_{ca} is the correlation time for the anionic motion. P is 1 and 2/3 for C_4 and C_3 reorientations, respectively [21]. We assumed C_3 reorientations for convenience.

The T_{2Q} data above 350 K were analyzed by (9a)–(9c), where b and d are fitting parameters. We used the τ_{c2} values obtained by the analysis of the $T_{1\varrho}$ data and the τ_{ca} values which was derived from T_{1Q} data (see Table 1). The results are shown in the insert of Fig. 1, where the best fitted curve is given by

$$T_{2Q}^{-1}/s^{-1} = 635 + 1.2 \times 10^8 \,\tau_{c2} + (3/2) \,\tau_{ca}^{-1}$$
. (10)

 $T_{\rm 2Q,latt}$, which is ascribed to the fluctuation due to lattice vibrations, was estimated to be 1.58 ms. Since the local magnetic field produced by protons is averaged by cationic motions, the interaction being fluctuated due to lattice vibrations is probably the local magnetic field produced by the chlorine and tin nuclei. We can estimate the one at a chlorine nucleus due to nearby four chlorine and one tin nuclei using (7). Since the Cl \cdots Cl and Sn \cdots Cl internuclear distances in the present complex are not available, average distances in some compounds including SnCl $_6^{2-}$ ions [22] were used. Internuclear distances of $r(\text{Cl} \cdots \text{Cl}) = 3.44 \,\text{Å}$ and $r(\text{Sn} \cdots \text{Cl}) = 2.43 \,\text{Å}$ lead to $T_{\rm 2Q}^{*} = 1.0 \,\text{ms}$. This value agrees well with $T_{\rm 2Q,latt}$ of 1.58 ms.

According to the BPP theory, an inverse of a square root of d, which is a fitting parameter of (9 b), has to be nearly equal to $(\gamma H_{loc})^{-1}$ or T_2'' [18]. The resulting value was 0.1 ms, which is nearly equal to the estimated values (0.08 ms) of T_{2Q}'' and T_{2Q} observed at low temperatures (0.45 ms).

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